# REGULAR UNIVERSITY EXAMINATIONS 2018/2019 ACADEMIC YEAR FOURTH YEAR FIRST SEMESTER 

SCHOOL OF SCIENCE BACHELOR OF SCIENCE IN APPLIED STATISTICS WITH COMPUTING

COURSE CODE: STA 420 COURSE TITLE: STATISTICAL DEMOGRAPHY

INSTRUCTIONS TO CANDIDATES

1. Attempt Question ONE and any other TWO questions.
2. Show all your Workings.

## QUESTION 1

a). In a stable population, the growth rate is $2 \%$ per annum, the death rate is 14.2 per a thousand and the value of

$$
\frac{{ }^{l_{15}}}{l_{0}}=0.7931
$$

i). What is the birth rate?
[2 Marks]
ii). What is the proportion of population aged 15 (that is aged between 15 and 16) years.
[3 Marks]
b). A part of a life table is provided below with some entries missing. On the basis of available information, complete the life table.

| Age | $l_{x}$ | $d_{x}$ | $q_{x}$ | $L_{x}$ | $T_{x}$ | $e_{x}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 93102 |  | 0.0062 |  |  |  |
| 11 |  |  | 0.0066 |  |  |  |
| 12 |  |  | 0.0072 |  |  |  |
| 13 |  |  | 0.0080 |  |  |  |
| 14 |  |  | 0.0090 |  |  |  |
| 15 |  |  | 0.0100 |  |  |  |
| 16 |  |  | 0.0112 |  |  |  |
| 17 |  |  | 0.0123 |  | 5027336 |  |

[5 Marks]
c). What is the Differentiate between
i). Fertility and Fecundity.
[2 Marks]
ii). Complete life table and Abridge life table.
[2 Marks]
iii). Gross Reproductive Rate (GRR) and Net Reproductive Rate (NRR).
[2 Marks]
d). In a certain life table

$$
\begin{aligned}
& \mu_{x}=0.15-0.10 x \text { for } 0 \leq x \leq \frac{1}{2} \text { and } \\
& \mu_{x}=0.10^{x} \text { for } \frac{1}{2} \leq x \leq 1 . \text { Find } l_{1} \text { if } l_{0}=100,000
\end{aligned}
$$

[4 Marks]
e). On the life table with, $l_{x}=\frac{100-x}{190}$.

Determine;
i). The chance that a child who has reached age 5 will live to 60 .
ii). The chance that a man of 30 lives to age 80 .
[1 Mark]
iii). The probability of dying within five years for a man aged 40.
[1 Mark]
iv). The average age of at death for those dying between ages 40and 45 .
[2 Marks]
v). The instantaneous death rate at age 40.
[1 Mark]
vi). The expectation of life at age 40.
[2 Marks]
vii). The chance that three men aged 30 at least one survives to age 80 .
[2 Marks]

## QUESTION 2

a). Find $l_{x}$ if $\mu_{x}=\frac{1}{100-x}$.
[4 Marks]
b). A group of lives experience special mortality between the ages 50 and 60 which can be represented by addition to the force of mortality according to the A 1967-70 mortality table ultimate of 0.01 at age 50 decreasing continuously in arithmetic progression to zero at age 60. Calculate the probability that a life aged 50 will live for 10 years.
[6 Marks]
c). The data provided below relates to an observed population

| Age Group | Female Population in ‘O00's | Births in 1000's |
| :--- | :---: | :---: |
| $15-19$ | 4459 | 19 |
| $20-24$ | 4383 | 427 |
| $25-29$ | 3974 | 674 |
| $30-34$ | 3540 | 318 |
| $35-39$ | 2949 | 185 |
| $40-44$ | 2663 | 22 |
| $45-49$ | 2418 | 1 |

A demographer also ascertains that the population is $91,088,000$ and the sex ratio of births is

$$
\frac{105 \text { Males }}{100 \text { Females }}
$$

Determine,
i). i). CBR.
[6 Marks]
ii). ii). TFR.
iii).iii). GRR.

## QUESTION 3

a). (i). A population satisfies the logistic law $\frac{d N}{d t}=r N-\lambda N^{2}$

Where $r>0$ and $\lambda>0$ are constants. At time $t_{0}$ it has $N_{0}$ members. Solve the differential equations by expressing the population as a fraction of time.
[8 Marks]
(ii). List the four fundamental laws of a stable population
[4 Marks]
(iii). Show that in a stationary population $b=\frac{1}{e_{0}}$ where b is the Birthrate and $e_{0}$ is the life expectancy at birth.
[4 Marks]
b). The following is the population characteristic of Lower Narok;

Population 1st January 201710554
Births
456
Deaths 215
Immigration
40
Emigration
145
Population 1st January 2018
Determine
i). The rate of growth during year 2017.
[2 Marks]
ii). The rate of Natural increase during the year 2017.
[2 Marks]

## QUESTION 4

a). The population of Mau Settlement Scheme satisfies the logistic law as provided in question 3 above where $\frac{d N}{d t}=r N-\lambda N^{2}$ with parameters $r=0.03$ and $\lambda=3 \times 10^{-8}$ And the time $t$ is measured in years. If the population in 2010 was 200,000
i). What was the population in the year 2030?
[7 Marks]
ii). What is the limiting value of the population
[2 Marks]
b). Two lives now aged $x$ and $y$ respectively are subjected to Gompertz Mortality from the same table where $\mu_{x}=B C^{x}$ and $\mu_{y}=B C^{y}$.
i). What is the probability that a life aged $x$ dies before the life aged ?
[10 Marks]
ii). Generalize the results in (i) for a case of three lives
[1 Mark]

