MAASAI MARA UNIVERSITY

School of Tourism \& Natural Resource Management
Department of Environment, Forestry \& Agriculture

## SECTION A: Answer all questions

Qn 1: What is a variable? Differentiate between quantitative and qualitative data. (3mks)
Qn 2: A Census Bureau report gave data on the number of times residents of Narok County had been married, for subjects of various ages. Table below summarizes responses for subjects of age 20 to 24 . The frequencies are in thousands of people, for instance, $7,074,000$ men never married.

Table 1: Number of Times Married, for Subjects of Age 20 to 24.

| Number of Times Married | Women | Men |
| :--- | :--- | :--- |
| 0 | 5861 | 7074 |
| 1 | 2773 | 1541 |
| 2 | 105 | 43 |

a) Find the median and the mean for each gender. Explain your answer. Which of these two measures of location is particularly more informative ( 5 mks )
b) Compute the standard deviation and the interquartile range for each gender. Which of these two measures of dispersion is particularly more informative ( 5 mks )
c) The following migration distances corresponding to distance moved by Pastoralist in search of pasture in kilometers were recorded as follows $43,6,7,11,122,41,21,17,1$, 3. Find the mean and standard deviation and then convert the first 3 observations to $\mathbf{Z}$ score. (7mks)

Qn 3: Given a simple regression with slope $b=3, S_{y}=8$, and $S_{x}=2$, find the standard error of the estimate ( 5 mks )

## SECTION B: Answer any 3 questions

Qn 4: A survey of the Native and immigrants population in Narok County reveals the following annual trip frequencies to the Mara National park.

$$
\begin{array}{ccc}
\bar{x}_{1}=4.1, & S_{1}^{2}=14.3, & n_{1}=20 \\
\bar{x}_{2}=3.1, & S_{2}^{2}=12, & n_{2}=16
\end{array}
$$

a) Assume that the variances are equal and test the null hypothesis that there is no difference between the park going frequencies of Native and immigrant population ( 5 mks )
b) Repeat the exercise assuming that the variances are unequal ( 5 mks )
c) Find the p-value associated with the test in part (a) and (b) (2mks)
d) Find a $95 \%$ confidence interval for the difference in means (3mks)

Qn 5: In an experiment to generate 500 data points, two simulations were done. The simulated variables were named Y 1 and Y 2 respectively. Please answer the following questions sequentially:
(a) Table below provide numerical summary of the two data sets. How useful are these summaries in describing the distributions for Y1 and Y2, respectively? Under what additional assumptions, do these summaries become useful? (4mks)

|  | Min | $1^{\text {st }}$ Quartile | Median | Mean | $3^{\text {rd }}$ Quartile | Max |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y1 | $\mathbf{- 4 . 8 0 4}$ | $\mathbf{3 . 3 6 9}$ | $\mathbf{6 . 1 9 8}$ | $\mathbf{6 . 1 3 3}$ | $\mathbf{9 . 1 2 9}$ | $\mathbf{1 7 . 3 2 0}$ |
| Y2 | $\mathbf{- 5 . 3 9 0 0}$ | $\mathbf{0 . 5 5 3 3}$ | $\mathbf{8 . 8 6 8 0}$ | $\mathbf{6 . 4 8 4 0}$ | $\mathbf{1 2 . 0 4 0 0}$ | $\mathbf{1 7 . 3 9 0 0}$ |

(b) Figure 1 below shows side-by-side notched boxplots for Y1 and Y2. Do these notched boxplots provide more information of these variables than the numerical summaries obtained in Part (a)? Are you totally confident with the graphical summary of the data based on the notched boxplots? Provide a detailed discussion. (4mks)


Figure 1: side by side notched box plot of simulation data for variables Y1 and Y2.
(c) Figure 2 below shows quantile plots for Y1 and Y2. Do the quantile plots provide more information of these variables than the notched boxplots? Are there any noticeable differences between these two data distributions? ( 4 mks )


Figure 2: quantile plot of $Y_{1}$ and $Y_{2}$ from simulated data.
(d) Provide a detailed discussion on the power of each technique used in part (a) to (c). What suggestions would you like to make in order to numerically or graphically summarize the data for a real problem in which no one knows the true distribution of the data? (3mks)

Qn 6: Using the following data,
Table 2: Annual swimming frequencies for three Kenyan cities

|  | Annual swimming frequencies |  |  |
| :--- | ---: | ---: | ---: |
|  | Nairobi | Kisumu | Mombasa |
|  | 38 | 58 | 80 |
|  | 42 | 66 | 70 |
|  | 50 | 80 | 60 |
|  | 57 | 62 | 55 |
|  | 80 | 73 | 72 |
|  | 70 | 39 | 73 |
| Mean | 32 | 73 | 81 |
| Standard deviation | 20 | 68 | 50 |
| $X_{++}=59.96 ; S^{2}=16.69$ | $\mathbf{4 8 . 6 3}$ | $\mathbf{6 3 . 6 3}$ | $\mathbf{6 7 . 6 3}$ |
|  | $\mathbf{1 9 . 8 8}$ | $\mathbf{1 2 . 6 6}$ | $\mathbf{1 1 . 4 3}$ |

a) Perform an analysis of variance to test that the swimming frequencies does no vary between the three cities. Show the between and within sum of squares, the observed $F$ statistic and the critical $F$ value ( 10 mks )
b) Use Levene's test to determine whether the assumption of homoscedasty is justified (5mks)

Qn 7: (a) find the correlation coefficient r , for the following sample data on education and income ( 2 mks )

| Observation | Income (Ksh) | Education (Years) |
| :--- | :--- | :--- |
| 1 | 30 | 12 |
| 2 | 28 | 12 |
| 3 | 52 | 18 |
| 4 | 40 | 16 |
| 5 | 35 | 16 |

(b). Test the null hypothesis that $\rho=0$ (5mk)
(c). Find the spearman rank correlation for these data ( 5 mks )
(d) Test whether the observed value of $\boldsymbol{r}_{s}$ is significantly different from zero ( 3 mks )

