

MAASAI MARA UNIVERSITY

REGULAR UNIVERSITY EXAMINATIONS 2022/2023 ACADEMIC YEAR THIRD YEAR FIRST SEMESTER

SCHOOL OF BUSINESS AND ECONOMICS BSC. ECONOMICS, FINANCIAL ECONOMICS &ECONOMICS & STATISTICS

COURSE CODE: ECO 3103-1
COURSE TITLE: ADVANCE MICROECONOMICS

DATE: 6/12/2023 TIME: 0830-1030 HRS

INSTRUCTIONS TO CANDIDATES

1. Answer Question **One** and any other **Two**questions.

This paper consists of **Three**printed pages. Please turn over.

Question One

In this exercise, we consider a utility maximization problem with a utility function that incorporates a taste for status. The utility function is

$$u(x, y) = (\alpha x^{\rho} + \beta y^{\rho})^{1/\rho} + \gamma M$$

That is, the utility function is the sum of a standard CES (Constant Elasticity of Substitution) utility function and the additional term γM . This extra term captures the fact that a higher income M raises directly the utility for this consumer by a factor γ , beyond any benefits in terms of allowing for purchases of x and y. (Assume $\gamma > 0$) Think of this as a 'status' effect: a higher income raises utility, for given consumption choices x and y: This function is well-defined for x > 0 and for y > 0: From now on, assume x > 0 and y > 0 unless otherwise stated. Assume $\alpha > 0$; $\beta > 0$ and $\rho < 1$: The price of good x is p_x the price of good y is p_y ; and the income of the consumer is M.

- a) Write down the budget constraint, assuming it is satisfied with equality.(2 marks)
- b) The consumer maximizes utility subject to the budget constraint as in (a). Write down the maximization problem of the consumer with respect to *x* and *y*. **(2 marks)**
- c) Write down the Lagrangean function and derive the first order conditions for this problem with respect to x, y; and λ .

(3 marks)

- d) Solve explicitly for x^* as a function of p_x , p_y and M. (4 marks)
- e) Solve explicitly for y^* as a function of p_x , p_y and M. (4 marks)
- f) Does the taste for social status γ affect the optimal choice for x^* , that is, does x^* depend on γ ? Are you surprised given the assumption of status effects? Provide intuition for this result. (2 marks)
- g) Using the solution in question (d), what is x^* in the special case $\rho = 0$? What utility function does CES correspond to for $\rho = 0$? In this case, are the goods substitutes or complements (or neither)? (3 marks).

Question Two

- a) What is meant by homogeneity of degree zero in consumer theory?(3 marks)
- b) What is money illusion? (3 marks)
- c) What is the relationship between (a) and (b)? (4 marks)

d) Given a Cobb-Douglas utility function below, derive its degree of homogeneity? (5 marks)

$$\mu(X_1 X_2) = A X_1^{\alpha} X_2^{\beta}$$

Question Three

Consider a firm using a technology described by the following production function

$$Q(K,L) = 2K^{1/2}L^{I/2}$$

Where K and L denote the amount of capital and labor used respectively. Assume that \mathbf{r} and \mathbf{w} are the prices of capital and labor respectively. Answer the following questions:

- a) Derive the conditional factor demand functions for this technology? (5 marks)
- b) Derive the cost function of the firm (5 marks)
- c) Demonstrate whether or not the cost function satisfies the usual properties. (5 marks)

Question Four

a) Consumer A derived the following demand function from a utility maximization problem. Calculate its price elasticity of demand.

(3 marks)

$$X_1 = \frac{1}{2} \frac{Y}{P_1}$$

- b) Consumers are assumed to have their self-interest of their own welfare and preference over commodities. Define consumer preference and describe its properties. (8 marks)
- c) Describe the regularity assumptions of a standard production technology.

(4 marks)