

## REGULAR UNIVERSITY EXAMINATIONS 2018/2019 ACADEMIC YEAR SECOND YEAR SECOND SEMESTER

## SCHOOL OF SCIENCE BACHELOR OF SCIENCE IN APPLIED STATISTICS WITH COMPUTING

# COURSE CODE: STA 2216 COURSE TITLE: FINANCIAL MATHEMATICS I

### **DATE: 15<sup>TH</sup> APRIL 2019**

**TIME: 1100 - 1300 HOURS** 

### **INSTRUCTIONS TO CANDIDATES**

- 1. Answer Question **ONE** and any other **TWO** questions.
- 2. Show all your Workings.

This paper consists of 4 printed pages. Please turn over.

#### QUESTION 1

- a) Define the term financial management and state the three decision functions that are vested with financial manager. [4 Marks]
- b) Differentiate between effective interest rate and Nominal interest rate.

[2 Marks]

c) Find the value at interest rate of 5 % per annum effective for the following functions;
[12 Marks]

(i) 
$$\ddot{a}_{\overline{65}}$$
 (ii)  $\ddot{s}_{\overline{62}}$  (iii)  $a_{\overline{63}}^{(4)}$  (iv)  $\overline{a}_{\overline{21}}$ 

d) John Grisham is considering investing in a security that has the following tribulations of possible one year returns:

Probability of	0.10	0.20	0.30	0.30	0.10
occurrence					
Possible returns	-0.10	0.00	0.10	0.20	0.30

What is the expected return and the standard deviation associated with the investment [6 Marks]

e) Suppose that the force of interest per annum at time t years is

$$\delta(t) = a \mathcal{C}^{-bt}$$

Show that the present value of 1 due at time t years is

$$v(t) = \exp\left[\frac{a}{b}\left(\mathcal{C}^{-bt} - 1\right)\right]$$
 [4 Marks]

f) Differentiate between the terms Annuity and Perpetuity as used in financial mathematics.
[2 Marks]

### QUESTION 2

a) Assume that  $\delta(t)$ , the force of interest per annum at time t (years), is given by the formula

$$\delta(t) = \begin{cases} 0.08 & 0 \le t < 5\\ 0.06 & 5 \le t < 10\\ 0.04 & t \ge 10 \end{cases}$$

Derive expressions for v(t), the present value of 1 due at time t

- b) An investor effects' a contract under which he will pay 15 premiums annually in advance into an account which accumulates according to the above force of interest. Each premium will be of amount £900 and the first premium will be paid at time 0. In return the investor will receive either
  - (i) The accumulated amount of the account one year after the final premium is paid: or
  - (ii) A level annuity payable annually for eight years, the first payment being made one year after the final premium is paid.
  - (iii) Find the lump sum payment under option (i) and the amount of the annual annuity under option (ii)

### [20 Marks]

### QUESTION 3

Two project proposals for electricity installation in an institution were presented to you as a financial advisor of a certain consultant firm;

**Project X:** delegates all installations tasks to a tendered company. The estimated cash flow for project X, are;

Time period	Estimated cost	Nature of charges
Beginning of year 1	(\$150,000)	Contactors fee
Beginning of year 2	(\$250,000)	Contactors fee
Beginning of year 3	(\$250,000)	Contactors fee
End of year 3	\$1,000,000	Sales

**Project Y:** proposes that all the installations work is done in-house by purchasing the required implements and use of own staff. The estimated cash-flow for this project are,

Time period	Estimated cost	Nature of charges	
Beginning of year 1	(\$325,000)	Staff cost	
Throughout year 1	(\$75,000)	Staff cost	
Throughout year 2	(\$90,000)	Staff cost	
Throughout year 3	(\$120,000)	Staff cost	
End of year 3	\$1,000,000	Sales	

Values in brackets indicates expenses or cash out flows, whereas in project Y the cost throughout the year are assumed to be spread evenly within the year.

**<u>Required:</u>** Discriminate between the two projects using;

(i). Net present Value, and	[10 Marks]
(ii). Internal rate of return	[10 Marks]

#### **QUESTION 4**

a) If  $\delta(t)$  and  $A(t_o, t)$  are continuous functions of t for  $t_o \le t$ , and the principle of consistency holds for  $t_o \le t_1 \le t_2$ . Proof that,

$$A(t_1, t_2) = \exp \int_t^{t_2} \delta(t) dt \,.$$
 [7 Marks]

b) Given that

 $\ddot{a}_{\overline{n}} = 7.029584$  and  $\ddot{a}_{2n} = 10.934563$ 

find the rate of interest *i* and duration *n*. [6 Marks]

c) A bank lends a company £ 5,000 at a fixed rate of interest of 10 % per annum. The loan is to be repaid by five level annual payments. Calculate the interest and capital payments at each repayment date.
[7 Marks]

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