# MAASAI MARA UNIVERSITY 

## REGULAR UNIVERSITY EXAMINATIONS 2018/2019 ACADEMIC YEAR FIRST YEAR SECOND SEMESTER EXAMINATION

# SCHOOL OF SCIENCE AND INFORMATION SCIENCE DEPARTMENT OF MATHEMATICS AND PHYSICAL SCIENCES 

## BACHELOR OF SCIENCE IN APPLIED STATISTICS WITH COMPUTING

COURSE CODE: STA 1208 COURSE TITLE: PRINCIPLES OF SAMPLE SURVEYS

## INSTRUCTIONS:

## SECTION ONE (30 MARKS)

a) Define the following terms as used in sample survey (6Marks)
i) Sample and population
ii) Sampling frame
iii) Purposive sampling and systematic sampling
iv) Parameter
b) Why do most researchers opt for using a sample in surveys as opposed to conducting a census 4marks)
c) Differentiate with examples and approaches given between probability sampling techniques from non-probability sampling? (6marks)
d) A Researcher has taken a small survey, using an SRS, for energy usage in houses. On the basis of the survey, each house is categorized as having electric heating or some other kind of heating. The January electricity consumption in kilowatt-hours for each house is recorded (Yi) and the results are given below: (8marks)

| Type of <br> Heating | Number of Sample Sample |  |  |
| :--- | :--- | :--- | :--- |
|  | Houses | Mean | Variance |
| Electric | 24 | 972 | 202,396 |
|  |  |  |  |
| Nonelectric | 36 | 463 | 96,721 |
| Total | 60 |  |  |

From recording existing, it is known that 16,450 of the 35,000 houses have electric heating, and 18,550 have nonelectric heating.
i) Using the sample, give an estimate and its standard error of the proportion of houses with electric heating. Does your $95 \%$ CI include the true proportion?
ii) Give an estimate and its standard error of the average number of kilowatt-hours used by houses in the city. What type of estimator did you use, and why did you choose that estimator?
e) Explain when a design may be considered as a cluster sample. What are the first-stage and second-stage units in cluster sampling of a country like Kenya?
(6marks)

## QUESTION TWO (20 MARKS)

A simple random sample of 1 in 20 households in a small town provided the following data about the availability of cars and the number of adults in household3.

| Number of cars <br> (Yi) in <br> the household | Adults in household <br> $(X i)$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | ---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | Total |
| 0 | 58 | 127 | 9 | 6 | 0 | 200 |
| 1 | 68 | 140 | 27 | 4 | 1 | 240 |
| 2 | 4 | 30 | 5 | 8 | 3 | 50 |
| 3 | 0 | 3 | 4 | 2 | 1 | 10 |
| Total | 130 | 300 | 45 | 20 | 5 | 500 |

a) Obtain point estimates, and approximate $95 \%$ confidence intervals for the following given that, $\sum \bar{x} \bar{y}=795$ ):
i. the total number of cars in the town's households, ii.the ratio of cars per adult in the town's households,
iii.the proportion of households with 1 or more cars per adult
b) A survey is to be conducted on the prevalence of the common diseases in a large population. For any disease that affects at least $1 \%$ of the individuals in the population, it is desired to estimate the total number of cases, with a coefficient of variation of not more than $20 \%$. What size of a simple random sample is needed, assuming that the presence of the disease can be recognized without mistakes?

## QUESTION THREE (20 MARKS)

(c) A campus population of size $N=9000$ is to be surveyed by a stratified sample for the prevalence of a certain disease, based upon three strata of respective sizes $N h=$ $1000,3000,5000$ for $h 1,2,3$. The costs of sampling individuals from these strata are estimated to be respectively 40,20 , and 10 USD per person. The campus health authorities believe that roughly $1 \%$ of stratum $1,5 \%$ of stratum 2 , and $12 \%$ of stratum 3 will test positive for the disease. I)
i) What is the optimal number of individuals to sample in each stratum if the total budget for data- collection in the survey is USD20000.
ii) Suppose that the same population were to be sampled by SRS. About how much would the SRS cost if you want to achieve the same MSE as in (a) in estimating the proportion of the population who have the disease ?
d) An opinion poll on Kenya's health concern was conducted by the Kenya National Aids Program between April 10-15, 2011. The survey reported that $89 \%$ of adults consider AIDS
as the most urgent health problem of the Kenya, with a margin of error of $\pm 3 \%$. The result was based on telephone interviews of 872 adults.
a. What was the target population?
b. What was the sample population?
c. How was the survey was conducted?
d. How was the sample selected?

## QUESTION FOUR (20 MARKS)

a) Foresters want to estimate the average age of trees in a stand in Mau forest. Determining age is cumbersome because one needs to count the tree rings on a core taken from the tree. In general, though, the older the tree, the larger the diameter, and diameter is easy to measure. The foresters measure the diameter of all 1132 trees and find that the population mean equals 10.3. They then randomly select 20 trees for age measurement.

| Tree No. | Diameter, x | Age, y | Tree No. | Diameter, x | Age, y |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 12.0 | 125 | 11 | 5.7 | 61 |
| 2 | 11.4 | 119 | 12 | 8.0 | 80 |
| 3 | 7.9 | 83 | 13 | 10.3 | 114 |
| 4 | 9.0 | 85 | 14 | 12.0 | 147 |
| 5 | 10.5 | 99 | 15 | 9.2 | 122 |
| 6 | 7.9 | 117 | 16 | 8.5 | 106 |
| 7 | 7.3 | 69 | 17 | 7.0 | 82 |
| 8 | 10.2 | 133 | 18 | 10.7 | 88 |
| 9 | 11.7 | 154 | 19 | 9.3 | 97 |
| 10 | 11.3 | 168 | 20 | 8.2 | 99 |
|  |  |  |  |  |  |

i) Estimate the population mean age of trees in the stand and give an approximate standard error for your estimate.
b) An accounting firm is interested in estimating the error rate in a compliance audit it is conducting. The population contains 828 claims, and the firm audits an SRS of 85 of those claims. In each of the 85 sampled claims, 215 fields are checked for errors. One claim has errors in 4 of the 215 fields, 1 claim has three errors, 4 claims have two errors, 22 claims have one error, and the remaining 57 claims have no errors.
i. Treating the claims as parameter 's and the observations for each field as sample's, estimate the error rate for all 828 claims. Give a standard error for your estimate.
ii.Estimate (with SE) the total number of errors in the 828 claims.

## QUESTION FIVE

a) Suppose we want to estimate the average number of hours of TV watched in the previous week for all adults in some county. Suppose also that the populace of this county can be grouped naturally into 3 strata (Nairobi, Kisumu, Sayepei(rural)) as summarized in the table

| Statistic Nairobi Kisumu | Sayepe(rural) |  |  |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
|  |  |  |  |
| $N h$ | 155 | 62 | 93 |
| $n h$ | 20 | 8 | 12 |
| $Y h$ | 33.90 | 25.12 | 19.00 |
| $S h$ | 5.95 | 15.24 | $9 . .36$ |
| $T h$ | 5254.5 | 1557.4 | 1767.0 |
| $C h$ | 2 | 2 | 3 |

(i) Compute a 95\% confidence interval for the total number of hours of TV watched in the previous week for all adults in this county.
(ii) Estimate the total sample size needed to estimate the mean hours of TV watched in this particular county to within 1 hour with $99 \%$ probability using optimal allocation (unequal and equal costs).
(b) A local radio station carries out regular polls of its listeners on items of current interest. In one such poll listeners were asked to telephone the station and just answer "yes" or "no" to the following questions.

Do you think the government of Kenya is serious in the fight against corruption?
The poll was carried out between 8 am and 9 am one morning. At 8:30 am the announcer said the percentage of "yes" vote was $63 \%$. When the poll closed at 9 am he announced that the percentage was $52 \%$. List two problems associated with this method of polling and suggest why each problem might cause misleading conclusion to be drawn.

## //END

